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## Looking at Functions

A function works like a machine. Numbers are put into the machine one at a time, and then the rule performs the operation(s) on each input to determine each output. For example, when $x=3$ is put into a machine with the rule $y=5 x-7$, the rule multiplies the input, 3 , by 5 and then subtracts 7 to get the output, which is 8 . This input and output can be written as an ordered pair: $(3,8)$. Then it can be placed on an $x y$-coordinate graph.
a. Find the output of the function machine at right when the input is $x=4$.
b. Likewise, find $y$ when $x=-1$ and $x=10$.
c. If the output of this relation is 45 , what was the input? That is, if $y=45$, then what is $x$ ? Is there more than one possible input?
inputs
$x=4$

outputs

8-118. Some relationships are special in that they are called functions. Below are two relationships, one of which $\left(y=x^{2}-2\right)$ is a function and the other, ( $x=y^{2}-2$ ), is not. Look at the graph and table of values below for each relationship and discuss with your team why you think the relationship in part (a) is a function and the one in part (b) is not. Use your ideas to create a definition of a function. Be prepared to share your ideas with the rest of the class. Use these questions to guide your discussion:
a. What is similar about the two relationships?
b. What is different about the two relationships?
c. What can we predict about the outputs for each relationship for a given input?

| $y=x^{2}-2$ |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $x$ | -3 | -2 | -1 | 0 | 1 | 2 | 3 |
| $y$ | 7 | 2 | -1 | -2 | -1 | 2 | 7 |



| $x=y^{2}-2$ |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $x$ | 7 | 2 | -1 | -2 | -1 | 2 | 7 |
| $y$ | -3 | -2 | -1 | 0 | 1 | 2 | 3 |



8-119. Examine each of the relationships below. Compare the inputs and outputs of each relation and decide if the relationship is a function. Explain your reasoning. Use your definition of a function from problem 8-118 to help you justify your conclusion.
a.

$$
\begin{array}{|c|c|c|c|c|c|c|c|}
\hline \boldsymbol{x} & 7 & -2 & 0 & 4 & 9 & -3 & 6 \\
\hline \boldsymbol{y} & 6 & -3 & 4 & 2 & 10 & -3 & 0 \\
\hline
\end{array}
$$

c.

e.

| $\boldsymbol{x}$ | $\boldsymbol{y}$ |
| :---: | :---: |
| -8 | 11 |
| 4 | 3 |
| 11 | -8 |
| 6 | 3 |
| -8 | 11 |

b.

| $\boldsymbol{x}$ | 3 | -1 | 2 | 0 | 1 | 2 | 9 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\boldsymbol{y}$ | 4 | -5 | 9 | 7 | 4 | -8 | 2 |

d.

f.


